

Name _____

Date _____

Advanced Algebra

Unit 6: I can solve a Matrix to System.

Assignment #13

You should use your answers and work from yesterday Assignment # 12

$$[A]^{-1} * [A] * \begin{bmatrix} a \\ b \\ c \\ d \end{bmatrix} = [A]^{-1} * [B]$$

$$\text{Therefore } \begin{bmatrix} a \\ b \\ c \\ d \end{bmatrix} = [A]^{-1} * [B]$$

So the KEY point to solving a matrix system is I need to know the Inverse Matrix. Then I am multiplying the inverse on both sides. The result is then getting the variable matrix by itself and multiplying two matrices on the other side. The result is the answer to the system.

$$1) \begin{bmatrix} 3 & -9 \\ -1 & 4 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \\ d \end{bmatrix} = \begin{bmatrix} 24 & -78 \\ -10 & 36 \end{bmatrix}$$

$$\text{So } \begin{bmatrix} \frac{4}{3} & 3 \\ \frac{1}{3} & 1 \end{bmatrix} \cdot \begin{bmatrix} 24 & -78 \\ -10 & 36 \end{bmatrix}$$

a= 2	b= 4
c= -2	d= 10

$$2) \begin{bmatrix} 1 & -2 \\ 2 & 1 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \\ d \end{bmatrix} = \begin{bmatrix} -8 & 4 \\ -1 & 13 \end{bmatrix}$$

$$\text{So } \begin{bmatrix} \frac{1}{5} & \frac{2}{5} \\ \frac{-2}{5} & \frac{1}{5} \end{bmatrix} \cdot \begin{bmatrix} -8 & 4 \\ -1 & 13 \end{bmatrix}$$

a= -2	b= 6
c= 3	d= 1

$$3) \begin{bmatrix} 3 & 2 \\ 5 & -4 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \\ d \end{bmatrix} = \begin{bmatrix} 24 & 70 \\ -70 & -30 \end{bmatrix}$$

$$\text{So } \begin{bmatrix} \frac{4}{22} & \frac{2}{22} \\ \frac{5}{22} & \frac{-3}{22} \end{bmatrix} \cdot \begin{bmatrix} 24 & 70 \\ -70 & -30 \end{bmatrix}$$

a= -2	b= 10
c= 15	d= 20

$$4) \begin{bmatrix} 3 & 2 \\ 9 & -5 \end{bmatrix} \begin{bmatrix} a & b \\ c & d \end{bmatrix} = \begin{bmatrix} -1 & 4 \\ -47 & -43 \end{bmatrix}$$

$$\begin{bmatrix} a & b \\ c & d \end{bmatrix} \text{ so } = \begin{bmatrix} \frac{5}{33} & \frac{2}{33} \\ \frac{9}{33} & \frac{-3}{33} \end{bmatrix} \begin{bmatrix} -1 & 4 \\ -47 & -43 \end{bmatrix}$$

④

$a = -3$	$b = -2$
$c = 4$	$d = 5$

$$5) \begin{bmatrix} 5 & -4 \\ 1 & 3 \end{bmatrix} \begin{bmatrix} a & b \\ c & d \end{bmatrix} = \begin{bmatrix} 5 & 30 \\ -18 & -32 \end{bmatrix}$$

$$\begin{bmatrix} a & b \\ c & d \end{bmatrix} \text{ so } = \begin{bmatrix} \frac{3}{19} & \frac{4}{19} \\ \frac{-1}{19} & \frac{5}{19} \end{bmatrix} \begin{bmatrix} 5 & 30 \\ -18 & -32 \end{bmatrix}$$

⑤

$a = -3$	$b = -2$
$c = -5$	$d = -10$

$$6) \begin{bmatrix} 4 & -3 \\ 7 & 12 \end{bmatrix} \begin{bmatrix} a & b \\ c & d \end{bmatrix} = \begin{bmatrix} -5 & -4 \\ 43 & 62 \end{bmatrix}$$

$$\begin{bmatrix} a & b \\ c & d \end{bmatrix} \text{ so } = \begin{bmatrix} \frac{12}{69} & \frac{3}{69} \\ \frac{-7}{69} & \frac{4}{69} \end{bmatrix} \begin{bmatrix} -5 & -4 \\ 43 & 62 \end{bmatrix}$$

⑥

$a = 1$	$b = 2$
$c = 3$	$d = 4$

$$7) \begin{bmatrix} 3 & 4 \\ -2 & 3 \end{bmatrix} \begin{bmatrix} a & b \\ c & d \end{bmatrix} = \begin{bmatrix} -27 & 58 \\ 40 & 18 \end{bmatrix}$$

$$\begin{bmatrix} a & b \\ c & d \end{bmatrix} = \begin{bmatrix} \frac{3}{17} & \frac{-4}{17} \\ \frac{8}{17} & \frac{-3}{17} \end{bmatrix} \begin{bmatrix} -27 & 58 \\ 40 & 18 \end{bmatrix}$$

⑦

$a = -14.2$	$b = 6$
$c = -10.2$	$d = 3.6$

$$8) \begin{bmatrix} 5 & -2 \\ 4 & 3 \end{bmatrix} \begin{bmatrix} a & b \\ c & d \end{bmatrix} = \begin{bmatrix} 4 & 52 \\ -6 & 36 \end{bmatrix}$$

$$\begin{bmatrix} a & b \\ c & d \end{bmatrix} = \begin{bmatrix} \frac{3}{23} & \frac{2}{23} \\ \frac{-4}{23} & \frac{5}{23} \end{bmatrix} \begin{bmatrix} 4 & 52 \\ -6 & 36 \end{bmatrix}$$

⑧

$a =$	$b =$
$c =$	$d =$

$$9) \begin{bmatrix} 7 & 2 \\ 3 & -5 \end{bmatrix} \begin{bmatrix} a & b \\ c & d \end{bmatrix} = \begin{bmatrix} 13 & 22 \\ -12 & -14 \end{bmatrix}$$

$$\begin{bmatrix} a & b \\ c & d \end{bmatrix} = \begin{bmatrix} \frac{5}{41} & \frac{2}{41} \\ \frac{3}{41} & \frac{-7}{41} \end{bmatrix} \begin{bmatrix} 13 & 22 \\ -12 & -14 \end{bmatrix}$$

⑨

$a =$	$b =$
$c =$	$d =$