

Advanced Algebra

Unit 7 Binomial Expansion Assignment #2

N=0	1
N=1	1 1
N=2	1 2 1
N=3	1 3 3 1
N=4	1 4 6 4 1
N=5	1 5 10 10 5 1

Evaluate the following Combinations:

1) ${}_{12}C_{10}$

$$\frac{12!}{10! 2!} = \frac{12 \times 11}{2} = 66$$

b) ${}_8C_5$

$$\frac{8!}{(8-5)! 5!} = \frac{8 \cdot 7 \cdot 6}{6} = 56$$

c) ${}_7C_5$

$$\frac{7!}{2! 5!} = \frac{7 \times 6}{2} = 21$$

n = 6 1 6 15 20 15 6 1
d) ${}_6C_2$

e) ${}_{10}C_8$

$$\frac{10!}{8! 2!} = \frac{10 \times 9}{2} = 45$$

f) ${}_5C_3$

$$\frac{5!}{2! 3!} = \frac{5 \times 4}{2} = 10$$

g) ${}_9C_6$

$$\frac{9!}{6! 3!} = \frac{9 \times 8 \times 7}{6} = 84$$

h) ${}_7C_0$

$$\frac{7!}{0! 7!} = 1$$

2) Use your Pascals triangle from your notes to expand out $(a+b)^6$

$$a^6 + 6a^5b + 15a^4b^2 + 20a^3b^3 + 15a^2b^4 + 6ab^5 + b^6$$

3) Using the pattern $(a+b)^5 = a^5 + 5a^4b + 10a^3b^2 + 10a^2b^3 + 5ab^4 + b^5$ to expand $(2x+3)^5$

$a = 2x$
 $b = 3$

$$(2x)^5 + 5(2x)^4(3) + 10(2x)^3(3)^2 + 10(2x)^2(3)^3 + 5(2x)(3)^4 + 3^5$$

$$32x^5 + 240x^4 + 720x^3 + 1080x^2 + 810x + 243$$

4) Given $(a+b)^8$, write down the 4th term

$$a^8 + a^7b + a^6b^2 + a^5b^3 + a^4b^4$$

Term 0 1 2 3 4

$${}_8C_4 = \frac{8!}{4!4!} = 70$$

$$70 a^4 b^4$$

5) Expand $(2+x)^4$ and simplify

$$2^4 + 4(2)^3x + 6(2)^2x^2 + 4(2)x^3 + x^4$$

$$16 + 32x + 24x^2 + 8x^3 + x^4$$

$$x^4 + 8x^3 + 24x^2 + 32x + 16$$

1 4 6 4 1

6) Use your pascals triangle to expand $(3x+4)^4$

$$(3x)^4 + 4(3x)^3 4 + 6(3x)^2 4^2 + 4(3x) 4^3 + 4^4$$

$$81x^4 + 432x^3 + 864x^2 + 768x + 256$$

7) Find the 4th term of $(2x+4)^6$

$${}^6C_4 (2x)^2 4^4$$

$$\frac{6!}{2!4!}$$

$$\frac{6 \times 5}{2}$$

$$15 \cdot 4x^2 \cdot 256$$

#7 final answer

$$15360x^2$$

8) Find the 6th term of $(3x+4)^8$

$${}^8C_6 (3x)^2 4^6$$

$$\frac{8!}{6!2}$$

$$\frac{8 \times 7}{2} = 28$$

$$28 \cdot 9x^2 \cdot 4096$$

$$1032192$$

#8 Final answer

$$1,032,192x^2$$

9) Find the 5th term of $(4x+12)^8$

$${}^8C_5 (4x)^3 12^5$$

$$\frac{8!}{5!3!}$$

$$\frac{8 \times 7 \times 6}{6} = 56$$

$$56 \cdot 64x^3 \cdot 248832$$

#9 Final answer

$$891813888x^3$$

10) Find the 8th term of $(2x+4)^{10}$

$${}^{10}C_8 (2x)^2 4^8$$

$$\frac{10!}{8!2!}$$

$$\frac{10 \times 9}{2} = 45$$

$$4x^2 (65536)$$

#10 Final answer

$$11,796,480x^2$$